

Option Pricing Class Problem Solution (Parts A and B)

Finance 4335, October 25, 2018

Ripple, Inc., stock is currently worth \$56. Each year, it can change by a factor of 0.9 or 1.3. The stock pays no dividends, and the annual continuously compounded risk-free interest rate is 4%.

- A. Calculate the price of a one-year European put option on Ripple, Inc. stock with an exercise price of \$60.

SOLUTION: We can solve this problem by via delta hedging and replicating portfolio approaches.

According to the Delta Hedging Approach:

$$\begin{aligned}P_u &= \text{Max}(0, K - S_u) = 0 \\P_d &= \text{Max}(0, K - S_d) = 9.6 \\V_H &= P + \Delta S = P + \Delta 56. \\V_H^u &= V_H^d \Rightarrow 0 + \Delta 72.80 = 9.60 + \Delta 50.40 \Rightarrow \Delta = .4286. \\V_H^u &= V_H^d = 31.20 \\V_H &= P + \Delta 56 = P + 24 = e^{-.04} 31.20 = .9608(31.20) = 29.98 \\P &= \$5.98\end{aligned}$$

According to the Replicating Portfolio Approach:

$$\Delta = \frac{P_u - P_d}{uS - dS} = \frac{0 - 9.60}{72.80 - 50.40} = -.4286; \text{ and } B = \frac{uP_d - dP_u}{e^{r\delta t}(u - d)} = \frac{1.3(9.60) - .9(0)}{1.0408(.4)} = 29.98. \text{ Then } V_{RP} = P = \Delta S + B = -.4286(56) + 29.98 = \$5.98.$$

- B. Calculate the price of a one-year European call option on Ripple, Inc. stock with an exercise price of \$60.

SOLUTION: We can solve this problem by via put-call parity, delta hedging, and replicating portfolio approaches. According to put-call parity,

$$C = P + S - Ke^{-r\delta t} = \$5.98 + \$56 - \$60e^{-.04} = \$4.33.$$

According to the Delta Hedging Approach:

$$\begin{aligned}C_u &= \text{Max}(0, S_u - K) = 12.80 \\C_d &= \text{Max}(0, S_d - K) = 0 \\V_H &= C - \Delta S = C - \Delta 56. \\V_H^u &= V_H^d \Rightarrow 12.80 - \Delta 72.80 = 0 - \Delta 50.40 \Rightarrow \Delta = .5714. \\V_H^u &= V_H^d = -28.80 \\V_H &= C - \Delta 56 = C - 32 = -e^{-.04} 28.80 = -.9608(28.80) = -27.67 \\C &= \$4.33\end{aligned}$$

According to the Replicating Portfolio Approach: $\Delta = \frac{C_u - C_d}{uS - dS} = \frac{12.80 - 0}{72.80 - 50.40} = .5714$ and $B =$

$$\frac{uC_d - dC_u}{e^{r\delta t}(u - d)} = \frac{1.3(0) - .9(12.80)}{1.0408(.4)} = -27.67. \text{ Then } V_{RP} = C = \Delta S + B = .5714(56) - 27.67 = \$4.33.$$