

STATISTICS CLASS PROBLEM SOLUTIONS (PROBLEMS 1-3)

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Suppose the return distributions for two risky assets are as follows:

<i>State</i>	p_s	$r_{a,s}$	$r_{b,s}$
1	1/3	-3%	36%
2	1/3	9%	-12%
3	1/3	21%	12%

1. Calculate the expected returns for assets a and b .

$$E(r_a) = \sum_{s=1}^n p_s r_{a,s} = (1/3)(-3\%) + (1/3)(9\%) + (1/3)(21\%) = 9\%$$

$$E(r_b) = \sum_{s=1}^n p_s r_{b,s} = (1/3)(36\%) + (1/3)(-12\%) + (1/3)(12\%) = 12\%$$

2. Calculate the variances and standard deviations for assets a and b .

$$\sigma_a^2 = \sum_{s=1}^n p_s (r_{a,s} - E(r_a))^2 = (1/3)(-3\% - 9\%)^2 + (1/3)(9\% - 9\%)^2 + (1/3)(21\% - 9\%)^2 = .96\%$$

$$\sigma_a = \sqrt{.96\%} = 9.8\%$$

$$\sigma_b^2 = \sum_{s=1}^n p_s (r_{b,s} - E(r_b))^2 = (1/3)(36\% - 12\%)^2 + (1/3)(-12\% - 12\%)^2 + (1/3)(12\% - 12\%)^2 = 3.84\%$$

$$\sigma_b = \sqrt{3.84\%} = 19.6\%$$

3. Calculate the covariance and correlation between assets a and b .

$$\begin{aligned} \sigma_{ab} &= \sum_{s=1}^n p_s (r_{a,s} - E(r_a))(r_{b,s} - E(r_b)) \\ &= (1/3)(-12\%)(24\%) + (1/3)(21\%)(-24\%) + (1/3)(12\%)(0) = -.96\% \end{aligned}$$

$$\rho_{ab} = \frac{\sigma_{ab}}{\sigma_a \sigma_b} = \frac{-.96\%}{(9.8\%)(19.6\%)} = -.50$$